## Problems Week 3

Due Monday, October 22, 2018

We've talked about least-squares fitting, and we've talked about the  $\chi^2$  distribution, so it's time to explore both more closely. Here we'll use wave height and wind speed data from buoys on the California coast. The data are available here:

https://www.ndbc.noaa.gov/historical\_data.shtml Download the data files for buoys 46025 and 46222 for 2015, 2016, and 2017.

1. **Visual evaluation.** Plot the time series of wind speed and wave height data from 46025 and wave height from 46222. Since the data are text files with a header, in Matlab you can read with:

## importdata

Read the help page. You'll want to specify a blank space delimiter between files and 2 header lines.

How are missing data identified in the records?

2. Monthly means. Since there's quite a bit of variability, average the data to produce monthly mean values. (You can average the three years together if you'd like.) Plot the means for each month and standard error of the mean. Data are provided at varying frequencies, but consecutive data are not independent. Assume that the wave data give you one independent sample per day and the wind speed data provide two independent samples per day. Hint: In Matlab, use:

## errorbar

to plot the data with uncertainty ranges.

- 3. Least-squares fit. Least-squares fit a mean and an annual cycle to the three data sets. What is the mean, and what is the amplitude of the annual cycle? (Total amplitude should be determined from the square root of the sum of the squares of the sine and cosine amplitudes.)
- 4. Least-squares fit a semi-annual cycle. Augment your annual cycle least-squares fit with a semi-annual cycle. What is the amplitude of the semi-annual cycle? Does the augmented fit give you a different annual cycle?
- 5.  $\chi^2$  and the misfit. What is the squared misfit of your least-squares fit? You can compute this as

$$\chi^2 = \sum_{i=1}^N \frac{(y_i - \sum_{j=1}^M a_{ij} x_j)^2}{\sigma_i^2} \sim N - M.$$
 (1)

In other words, the misfit for each point should be roughly equal to the uncertainty. We lose a degree of freedom for each function that we use to fit. How much does the misfit change if you fit with an annual cycle only or with an annual

plus semi-annual cycle? Use the  $\chi^2$  distribution to evaluate whether your fits are improved by adding the semi-annual fit? On the basis of the  $\chi^2$  distribution, are you overfitting the data, or choosing the wrong model for your data?