

$$\omega(r, k) = v(r) \cdot k + \sqrt{g |k|}$$