

$$\ddot{\mathbf{r}} = \nabla \left( \frac{1}{2} |\mathbf{v}|^2 \right) + \zeta \hat{\mathbf{z}} \times \dot{\mathbf{r}} + \dot{\beta} (\dot{\mathbf{r}} - \mathbf{v})$$