

$$\beta(k) \stackrel{\text{def}}{=} \ln \left(\frac{\bar{\omega}_k}{k} \right)$$