

$$\chi \dot{s}^2 = \zeta \dot{s} + \hat{n} \cdot \nabla \left(\frac{1}{2} |v|^2 \right) - \dot{\beta} \hat{n} \cdot v$$