$$\chi \dot{s}^2 = \zeta \dot{s} + \hat{\boldsymbol{n}} \cdot \nabla \left(\frac{1}{2} |\boldsymbol{u}|^2 \right) - \dot{\beta} \, \hat{\boldsymbol{n}} \cdot \boldsymbol{u}$$