

$$x = \frac{\zeta}{\bar{\omega}_k} + O\left(\frac{u}{\bar{\omega}_k}\right)^2$$