

$$S = \int_{-\infty}^0 u_s dz = \frac{1}{2} a^2 kc$$