

$$\begin{aligned} \mathcal{U}_L &\stackrel{\text{def}}{=} \bar{\chi}, \\ &= \epsilon^2 \bar{u}_2 + \epsilon^2 c e^{2kz} \end{aligned}$$