

$$a_z = 0^- : \quad \underbrace{\bar{v}}_{= \bar{\phi}_z} = -S_x$$